

**Homework #2 - To be handed in no later than 2:41 p.m., Monday, May 22**

1. Let  $X$  be the plane and let  $\mathbf{B}$  be the collection of all circles centered at the origin, including the origin itself—that is, the circle of radius 0. Show that  $\mathbf{B}$  is a base for a topology on  $X$ , and find the closure and the interior of the square

$$S = \{(x, y) : -1 \leq x \leq 1, -1 \leq y \leq 1\}.$$

2. Let  $(X, d)$  be a pseudometric space. Show there is a pseudometric  $\rho$  on  $X$  that is equivalent to  $d$  and has the property that there is a real number  $M$  such that  $\rho(x, y) < M$  for all  $x$  and  $y$  in  $X$ .