

**Homework #4- Hand in no later than 2:41 p.m., Friday, May 26**

Let  $X$  be the plane and define pseudometrics  $d$  and  $\rho$  by

$$d(x, y) = \sqrt{(x_1 - y_1)^2 + (x_2 - y_2)^2}, \text{ and}$$
$$\rho(x, y) = |x_1 - y_1|;$$

where, of course,  $x = (x_1, x_2)$  and  $y = (y_1, y_2)$ . Let  $i$  be the identity function on  $X$ ; that is,  $i(x) = x$  for every  $x \in X$ . Prove or disprove:

1.  $i : (X, \rho) \rightarrow (X, d)$  is continuous.

2.  $i : (X, d) \rightarrow (X, \rho)$  is continuous.